2018 James S. Rickards Fall Invitational

Mental Math

Name:
School:
Score:

- 1. _____ What is the value of $< -23, 15, 16 > \cdot < 17, -4, 37 > ?$
- 2. _____ How many zeroes are there in the base 7 representation of 3500!?
- 3. _____ What is the sum of the cubes of the roots in the function $f(x) = 2x^2 6x + 3$?

4. What is the product of the eigenvalues of the following matrix: $\begin{bmatrix} 2 & -4 & 3 \\ -4 & 5 & 7 \\ 4 & 2 & -2 \end{bmatrix}?$

- 5. _____ What is the sum of the fifth hexagonal number and seventh pentagonal number?
- 6. _____ Find the remainder when 13^{32} is divided by 11.
- 7. _____ How many digits are in the expansion of 5^{37} ?
- 8. _____ What is the volume of a regular tetrahedron with side length of 11?
- 9. _____ How many positive integers are relatively prime to and less than 693?
- 10. _____ What is the length of the segment that is parallel to the bases and divides a trapezoid into two equal areas given that the lengths of the bases are 13 and 21?
- 11. _____ What is the sum of the squares of the reciprocals of the roots of the function $f(x) = 4x^4 3x^3 + 7x^2 14$?
- 12. _____ How many petals are on the curve $r = \cos\left(\frac{7}{6}\theta\right)$?
- 13. _____ What is the maximum number of possible negative real roots in the function $f(x) = -9x^9 3x^7 + 6x^6 3x^5 3x^4 + 2x^2 5?$
- 14. _____ What is the product of the slopes of the asymptotes of the following conic: $-16y^2 36x + 9x^2 96y 252 = 0$?
- 15. _____ How many holes does the following function have? $f(x) = \frac{(x-7)^2(x-3)^5(x-1)^9(x-\pi)^2(x-5)(x-11)^4}{(x-\pi)^2(x-3)^6(x-2)(x-1)(x-7)}$
- 16. _____ How many minutes are in 42 full days?
- 17. _____ What is the third term in the expansion of $(3-2x)^{-5}$?
- 18. _____ What is the sum of the positive integer factors of 1080?
- 19. _____ What is the sum of the coefficients of the expansion $(3x^2 + 5y^6 + 7z^{10})^2$?
- 20. _____ What is the minimum of $f(x) = 3x^4 9x^2 + 14?$
- 21. _____ What is 16^3 ?
- 22. _____ What is $\cos(\frac{\pi}{2}) \times 1.5$?
- 23. _____ What is the value of $10 12 \times 14 + 16$?
- 24. _____ What is the sum of the reciprocals of the first four prime numbers?
- 25. _____ What is the sum of the first 10 positive odd integers?
- 26. _____ How many different ways can a group of 6 distinguishable children be arranged?
- 27. _____ One of the sides of a right triangle having all integer sides is 11. What is the hypotenuse?
- 28. _____ What is the degree measure of one internal angle of a 14 sided regular polygon, rounded to the nearest tenth?

- 29. _____ What is the sum of the 14th and 17th Fibonacci numbers, if the first Fibonacci number is 0?
- 30. _____ What is the sum of the positive prime factors of 1485.
- 31. _____ Simplify $\sqrt{8064}$ into simplest radical form.
- 32. _____ What is the product of the 8th and 9th triangle numbers?
- 33. _____ What is the LCM of 21, 19, and 14?
- 34. _____ Find the arithmetic mean of the following set of numbers: 12, 4, 6, 8, 24, 7, 4, 9, 3, 25, 14, 16
- 35. _____ What is 2018 * 2018?
- 36. _____ In how many ways can the letters of the word "Rickards" be arranged?
- 37. _____ What is the value of 27 + 35?
- 38. _____ How many times does the number 8 appear in at least one digit of the first 1000 positive integers?
- 39. _____ A depressed teenager sleeps 13 hours a day. How many hours does the teen sleep in a non leap year?
- 40. _____ What is the slope of the line going through the points (-4, 13) and (2, 15)?